- 1 Citation: Hirt C, Kuhn M, Featherstone WE, Göttl F (2012) Topographic/isostatic evaluation of new-generation
- 2 GOCE gravity field models, J. Geophys. Res., 117, B05407, doi:10.1029/2011JB008878
- 3

4 Topographic/isostatic evaluation of new-generation 5 GOCE gravity field models

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7 **C. Hirt**

- 8 Western Australian Centre for Geodesy & The Institute for Geoscience Research,
- 9 Curtin University of Technology, GPO Box U1987, Perth, WA 6845, Australia
- 10 Email: <u>c.hirt@curtin.edu.au</u>
- 11

12 **M. Kuhn**

- 13 Western Australian Centre for Geodesy & The Institute for Geoscience Research,
- 14 Curtin University of Technology, GPO Box U1987, Perth, WA 6845, Australia
- 15 Email: <u>m.kuhn@curtin.edu.au</u>
- 16

17 W.E. Featherstone

- 18 Western Australian Centre for Geodesy & The Institute for Geoscience Research,
- 19 Curtin University of Technology, GPO Box U1987, Perth, WA 6845, Australia
- 20 Email: <u>w.featherstone@curtin.edu.au</u>
- 21
- 22 **F. Göttl**
- 23 Deutsches Geodätisches Forschungsinstitut (DGFI),
- 24 Alfons-Goppel-Strasse 11, 80539 München, Germany
- 25 Email: goettl@dgfi.badw.de
- 26

27 Abstract We use gravity implied by the Earth's rock-equivalent topography (RET) and 28 modeled isostatic compensation masses to evaluate the new global gravity field models 29 (GGMs) from European Space Agency (ESA)'s Gravity Field and Steady-State Ocean 30 Circulation Explorer (GOCE) satellite gravimetry mission. The topography is now 31 reasonably well-known over most of the Earth's land masses, and also where conventional 32 GGM evaluation is prohibitive due to the lack (or unavailability) of ground-truth gravity data. 33 We construct a spherical harmonic representation of Earth's RET to derive band-limited 34 topography-implied gravity, and test the somewhat simplistic Airy/Heiskanen and 35 Pratt/Hayford hypotheses of isostatic compensation, but which did not improve the agreement 36 between gravity from the uncompensated RET and GOCE. The third-generation GOCE 37 GGMs (based on 12 months of space gravimetry) resolve the Earth's gravity field effectively 38 up to spherical harmonic degree ~200-220 (~90-100 km resolution). Such scales could not be 39 resolved from satellites before GOCE. From the three different GOCE processing 40 philosophies currently in use by ESA, the time-wise and direct approaches exhibit the highest 41 sensitivity to short-scale gravity recovery, being better than the space-wise approach. Our 42 topography-implied gravity comparisons bring evidence of improvements from GOCE to gravity field knowledge over the Himalayas, Africa, the Andes, Papua New Guinea and
Antarctic regions. In attenuated form, GOCE captures topography-implied gravity signals up
to degree ~250 (~80 km resolution), suggesting that other signals (originating, e.g., from the
crust-mantle boundary and buried loads) are captured as well, which might now improve our

47 knowledge on the Earth's lithosphere structure at previously unresolved spatial scales.

48

49 Keywords GOCE, topography, gravity, rock-equivalent topography, isostasy

50

51 **1 Introduction**

The Gravity Field and Steady-State Ocean Circulation Explorer (GOCE) is the first core mission of the "Living Planet" Earth observation programme by the European Space Agency (ESA), e.g., *Drinkwater et al.* [2003]. The GOCE satellite was launched in March 2009 and entered its operational phase in September 2009. GOCE is the first mission to carry a dedicated on-board three-axis gravity gradiometer at a low orbit altitude of ~260 km [*Bock et al.*, 2011] attempting to resolve Earth's external gravity field with unprecedented detail from space.

59 GOCE gravity field determination is based on the combination of satellite gravity 60 gradiometry (SGG) with satellite-to-satellite tracking (SST). SGG, used to measure the second derivatives of the gravitational potential, is very sensitive to the medium-wavelength 61 62 components of the gravity field [e.g., Rummel et al., 2011]. In solid-Earth geophysics, 63 GOCE SGG is expected to resolve regional mass-density anomalies that carry information on 64 the Earth's interior [e.g., Marotta, 2003; Bagherbandi, 2011; Reguzzoni and Sampietro 65 2012]. GPS-based SST provides high-accuracy information on the GOCE satellite orbit geometry [Bock et al., 2011] to complement the GOCE SGG in the long wavelengths. 66 67 GOCE's repeat cycle (the period to achieve full global data coverage) is ~2 months, and the 68 envisaged data collection period is expected to total ~40 months, from September 2009 til 69 December 2012 and possibly longer.

70 GOCE's mission target was to map gravity field features with 1-2 cm accuracy for 71 geoid undulations and ~1 mgal for gravity, down to scales of ~100 km, or spherical harmonic 72 degree ~200. By comparison, geoid undulations from the EGM2008 global geopotential 73 model (GGM) [Pavlis et al., 2008] are estimated to be accurate at the ~7 cm level (global 74 RMS). Over gravimetrically well-surveyed areas, the EGM2008 geoid accuracy can be at the 75 level of some cm [e.g., Hirt et al., 2010a], while the accuracy degrades to the dm-level over large parts of Asia, Africa, South America and Antarctica [Pavlis et al., 2008]. 76 In these 77 EGM2008 'problem areas', Pavlis et al. [2008] did not have high-resolution terrestrial 78 gravity data (12% of land) or only had access to proprietary data (43% of land). It is these 79 regions devoid of dense sets of terrestrial gravity observations where GOCE is expected to 80 add most significantly to terrestrial gravity field knowledge.

ESA has made available GOCE GGMs based on ~2 months (herein first-generation), ~8 months (second-generation) and ~12 months (third-generation) of observation data, based on three different strategies for gravity field recovery [e.g., *Pail et al.*, 2011], see Section 2. The performance of the first-generation GGMs has been evaluated by different strategies. *Gruber et al.* [2011] investigated GOCE-implied orbit residuals of various geodetic satellites and compared GOCE GGMs against ground-truth geoid undulations. *Hirt et al.* [2011] utilized regional land gravity and vertical deflections as ground-truth to assess GOCE gravity field information. Differences between GOCE GGMs and EGM2008 (from the pre-GOCEera) were analysed by *Hirt et al.* [2011] and *Pail et al.* [2011], and inferences were made but no direct evidence obtained for GOCE-conferred improvements over the EGM2008 'problem areas'.

92 The aim of this study is to use gravity implied by the Earth's topography and models 93 of its isostatic compensation masses to assess the new-generation GOCE model performance 94 over the Himalayas, Africa, Andes, Papua New Guinea and Antarctica. We exploit the 95 relatively good knowledge of topography over most of the Earth's surface (through digital 96 elevation models) along with GOCE's sensitivity to the gravitational attraction of 97 topographic masses [Wild and Heck, 2005; Makhloof and Ilk 2008; Janák et al., 2012] to 98 bring - for the first time - direct evidence for GOCE gravity field improvements in regions 99 where terrestrial gravity data are restricted.

100 Based on topographic heights over land areas, ocean depths, ice shield thickness data, we construct rock-equivalent topography (RET; Rummel et al. [1988]) and derive RET-101 102 implied gravity to approximate the gravitational attraction of Earth's topography and some of 103 Earth's major mass-density anomalies. Some focus is placed on ways to account for isostatic 104 compensation of the topography [e.g., Watts, 2001]. The gravitational effect from the 105 isostatic compensation masses is approximated and tested here based on the Crust 2.0 106 lithosphere model [Bassin et al., 2000], the classical Airy/Heiskanen and Pratt/Hayford 107 hypotheses and a combination of them (Section 3). The relationship between GOCE-108 measured and topography/isostasy-implied gravity is not only analyzed using correlation 109 coefficients, but also based on a new criterion termed reduction rates. These quantify the 110 extent of topography-implied gravity signals captured by the GOCE GGMs at different 111 spatial scales (i.e., as a function of harmonic degree). Reduction rates are introduced and used because they are more sensitive than correlation coefficients to identify topography-112 113 generated signals in the GGMs (Section 4).

Gravity implied by RET not only allows for identification of GOCE-conferred gravity 114 115 field improvements over EGM2008 'problem areas', but also global and regional evaluation 116 of the GOCE gravity recovery strategies. Using RET as a single, globally homogeneous reference data set, our analyses provide independent feedback on the ability of the ESA 117 GOCE gravity processing strategies to recover short-scale gravity signals. While Pail et al. 118 119 [2011] state that "due to the fact that the [three] models are based on different processing 120 philosophies [...] they cannot and should not be compared directly", we believe that users are 121 interested to know how the different GOCE models perform both in an absolute and relative 122 sense. Comparisons between uncompensated and compensated RET demonstrate that the 123 classical hypotheses of isostatic compensation are of limited use to model isostasy globally at 124 the spatial scales resolved by GOCE. Comparisons with uncompensated RET-implied 125 gravity show the performance differences of the three GOCE gravity recovery strategies, and 126 demonstrate the sensitivity of GOCE gradiometry for short-scale gravity recovery at spatial 127 scales down to ~80 km, which also has future applications in solid Earth geophysics, e.g., the 128 improvement of lithosphere models at short scales (Sections 4, 5).

- 129
- 130 **2 Data sets**
- 131 2.1 GOCE Gravity Field Models
- 132
- 133 **Table 1.** Global gravity field models tested
- 134

Model name	Degree	GOCE Data	Other data ⁱ	Reference	
GOCE-DIR3 ^a	240	~12 months	LAGEOS and GRACE to	Bruinsma et al. (2010)	
			degree 160 from GRGS RL02		
			(Bruinsma et al. 2009)		
GOCE-DIR2 ^b	240	8 months	ITG-Grace2010s	Bruinsma et al. (2010)	
			to degree 150		
GOCE-DIR1 ^c	240	2 months	EIGEN51C (GRACE,	Bruinsma et al. (2010)	
			CHAMP, G,A)		
			at all scales		
GOCE-SPW2 ^d	240	8 months	N/A	Migliaccio et al. (2010)	
GOCE-SPW1 ^e	210	2 months	EGM2008 (GRACE, G,A)	Migliaccio et al. (2010)	
			at low degrees		
GOCE-TIM3 ^f	250	~12 months	N/A	Pail et al. (2011)	
GOCE-TIM2 ^g	250	8 months	N/A	Pail et al. (2011)	
GOCE-TIM1 ^h	224	2 months	N/A	Pail et al. (2010)	
ITG-Grace2010s	180	-	7 years GRACE	Mayer-Gürr et al. (2010)	

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136			
137	а	ESA name	GO_CONS_EGM_GCF_2_20091101T000000_20110419T235959_0001
138		ICGEM name	GOC_CONS_GCF_2_DIR_R3
139	b	ESA name	GO_CONS_EGM_DIR_2I_20091101T000000_20100630T235959_0001
140		ICGEM name	GOC_CONS_GCF_2_DIR_R2
141	c	ESA name	EGM_GOC_2_20091101T000000_20100110T235959_0002
142		ICGEM name	GOC_CONS_GCF_2_DIR_R1
143			
144	d	ESA name	GO_CONS_EGM_SPW_2I_20091031T000000_20100705T235959_0001
145		ICGEM name	GOC_CONS_GCF_2_SPW_R2
146	e	ESA name	EGM_GOC_2_20091030T005757_20100111T073815_0002
147		ICGEM name	GOC_CONS_GCF_2_SPW_R1
148			
149	f	ESA name	GO_CONS_EGM_GCF_2_20091101T000000_20110430T235959_0001
150		ICGEM name	GOC_CONS_GCF_2_TIM_R3
151	g	ESA name	GO_CONS_EGM_TIM_2I_20091101T000000_20100705T235500_0001
152		ICGEM name	GOC_CONS_GCF_2_TIM_R2
153	h	ESA name	EGM_GOC_2_20091101T000000_20100111T000000_0002
154		ICGEM name	GOC_CONS_GCF_2_TIM_R1
155	i	Abbreviations: G	$\dot{\mathbf{b}}$ = terrestrial gravity, A = gravity from altimetry.
156			
157		The spherical	harmonic coefficients of eight GOCE-based GGMs from the GOCE
158	High-I	Level Process	ing Facility (HPF) have been released publically via ESA
159	(http://	/www.esa.int)	and the International Centre for Global Earth Models (ICGEM,
160	http://i	cgem.gfz-potsc	lam.de/ICGEM/). Table 1 gives an overview of their formal resolution

161 (i.e., the maximum spherical harmonic degree published), the data used to derive the model

162 coefficients, and the corresponding citations. As a benchmark of the pre-GOCE-era, one
163 GRACE (Gravity and Climate Change Experiment; *Tapley et al.* [2004])-based model (ITG164 GRACE2010s, using seven years of GRACE observations, cf. *Mayer-Gürr et al.* [2010]) is
165 also included.

The eight GOCE GGMs are based on three different processing philosophies [*Pail et al.*, 2011]: the direct approach (DIR), space-wise approach (SPW) and time-wise approach (TIM). Each approach has been applied to ~2 months (first-generation), ~8 months (secondgeneration) and ~12 months (third-generation) of GOCE gradiometry and GPS-derived orbits. Below are the basic concepts and most important differences among the approaches, inferred from *Pail et al.* [2011] and the header information in the coefficient files from ICGEM.

- The DIR and TIM approaches use the least-squares solution of the inverse problem,
 where GOCE observations (gradiometry and GPS orbits) are related to the unknown
 parameters (spherical harmonic coefficients of Earth's gravity field) via large systems of
 normal equations. Their direct inversion generally requires the use of supercomputers.
- 177 • The DIR-approach makes use of an a priori GGM (cf. Table 1) and adds GOCE 178 observations to improve it. An important difference between first- and second/third-179 generation DIR models, GOCE-DIR1 incorporates a priori information from the 180 combined EIGEN-51C model [Bruinsma et al., 2010] at all spatial scales. As such, GOCE-DIR1 relies on other satellite data at long scales and terrestrial gravity at short 181 182 Opposed to this, GOCE-DIR2 uses the GRACE-only-derived model ITGscales. 183 GRACE2010s (cf. Table 1) as an *a priori* GGM to degree 150, so is a pure GOCE-only GGM beyond this degree. GOCE-DIR3 uses LAGEOS Satellite Laser Ranging and the 184 185 GRGS GRACE model [Bruinsma et al., 2009] gravity field as an a priori to degree 160.
- No *a priori* gravity field information is used in the GGMs derived from the TIM approach, but Kaula regularisation (an empirical law on the decay of the Earth's gravity spectrum with altitude, cf. *Kaula* [1966]) is applied to constrain the TIM1, TIM2 and TIM3 GGM coefficients at short scales. The TIM processing philosophy delivers pure GOCE-only models that are independent of *a priori* gravity field data.
- In the SPW approach, GOCE observations are gridded at satellite altitude by means of least-squares collocation. The spherical harmonic coefficients are obtained through a spherical harmonic analysis of the gridded observations. EGM2008 is incorporated into GOCE-SPW1 as an *a priori* model only at very long wavelengths, so it can be considered as a pure GOCE-only model at medium and shorter scales. According to the ICGEM file information, GOCE-SPW2 does not use *a priori* gravity field information.
 GOCE-SPW3 is not yet publicly available.
- In summary, GOCE-TIM1,2&3 and GOCE-SPW2 are pure GOCE-only models at all
 spatial scales, and GOCE-SPW1 is GOCE-only apart from the very long wavelengths.
 GOCE-DIR2,3 are GOCE-only models at short scales and GOCE-DIR1 is a mixed product
 that is underpinned by various prior gravity field sources.
- We acknowledge that 'combined satellite-only' GGMs (e.g., GOCO01S, *Pail et al.* [2010], GOCO02S, *Goiginger et al.* [2011] and EIGEN-6, *Förste et al.* [2011]) have been developed based on GOCE and GRACE. Such GGMs are superior to GOCE-only models

due to incorporating highly-accurate GRACE models at long wavelengths (and/or other satellite data), cf. *Pail et al.* [2010]. Given that the GOCE component of these combined satellite-only GGMs is similar or identical to the ESA GOCE products, we limit our study to the GGMs in Table 1.

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210 **2.2 Topography**

211 We use the spherical harmonic expansion of the DTM2006.0 digital elevation data [Pavlis et al., 2007], a co-product of EGM2008 [Pavlis et al., 2008]. It contains (i) the 212 213 Shuttle Radar Topography Mission (SRTM, Farr et al., [2007]) data over land within 214 latitudes of 56° South and 60° North, (ii) ICESat-2 laser altimetry [Abdalati et al., 2010] over 215 Greenland and Antartica, (iii) bathymetry derived from altimetry and ship depth soundings 216 [Smith and Sandwell, 1997], and (iv) DTM2002 elevation data [Saleh and Pavlis, 2003] 217 elsewhere. Spherical harmonic coefficients of the topography, derived to degree 2700 from 218 2'×2' DTM2006.0 mean values, are publicly available to degree 2160 via http://earth-219 info.nga.mil/GandG/wgs84/gravitymod/egm2008/.

220 In order to better RET-model the ice sheets over Greenland and Antarctica, we use the 221 bedrock information contained in the global $1' \times 1'$ ETOPO1 relief model [Amante and Eakins, 222 2009]. Over Greenland, bedrock elevations are obtained indirectly through ice surface and 223 ice thickness information provided by the National Snow and Ice Data Centre (NSIDC) 224 [Bamber et al., 2001]. The ice surface is the result of the combination of radar altimetry and 225 airborne data, where the ice thickness is obtained from airborne ice-penetrating radar. Over 226 Antarctica, BEDMAP describes the bedrock elevation under the grounded ice sheets [Lythe et 227 al., 2000]. This is based primarily on the gridding of radar and seismic soundings.

228

229 3 Methodology

230 **3.1 Introductory Remarks**

231 The basic idea of this study is to compare gravity signals, as measured by GOCE and 232 implied by Earth's topography and models of its isostatic compensating masses, at various 233 spatial scales. For this purpose, we construct a spherical harmonic representation of Earth's 234 topography, cryosphere and hydrosphere based on a uniform mass-density (Section 3.2), 235 derive its gravitational potential (Section 3.3) and gravity disturbances (Section 3.4) that are compared over a range of spectral bands (Section 4), allowing us analyses of GOCE's 236 237 sensitivity for topography-generated gravity signals, specifically at short spatial scales that 238 have never been measured from space before.

239 GOCE is not only sensitive to the gravitational attraction of the Earth's visible 240 topography, but also to its isostatic compensation masses [e.g., Wild and Heck, 2005; 241 Makhloof and Ilk, 2008]. This raises the question of how to account for isostatic 242 compensation in the comparisons between GOCE and Earth's topography. An initial strategy 243 is to consider the topography as isostatically uncompensated or supported by the rigidity of 244 the lithosphere, which, according to Wieczorek [2007], should be a "good approximation" 245 above harmonic degree ~200. To model isostatic compensation of the topographic masses, 246 commonly used strategies are available that are based on

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Simplistic compensation models, such as those of Airy-Heiskanen (A/H) or Pratt-248 249 Hayford (P/H) [e.g., Heiskanen and Moritz, 1967; Torge, 2001; Göttl and Rummel 250 2009]. The A/H and P/H models (Section 3.3) assume local compensation of the topography loads and an intrinsically weak crust [e.g., Watts, 2001], so are sometimes 251 252 crude simplifications of the actual lithospheric properties. It is important to note that 253 both the A/H and P/H compensation models offer [formally] a spatial resolution 254 comparable to that of the topography model, so possess short-scale spectral energy 255 which is a prerequisite for comparisons with GOCE.

- More regional compensation models of Vening-Meinesz also take into account the flexural rigidity of the lithosphere [e.g., *Watts*, 2011]. Regional compensation models imply that loads larger than a certain transition wavelength are compensated while smaller topographic features are supported mechanically by the lithosphere. The transition wavelength depends upon, among other parameters, the elastic thickness T_e .
- Crustal thicknesses estimates, e.g., from seismic refraction data such as the Crust 2.0 lithosphere model [*Bassin et al.*, 2000], or effective elastic thickness estimates from admittance and coherence studies [e.g., *Watts*, 2001, p 416f]. However, neither the Crust 2.0 resolution (2°×2° corresponding to spherical harmonic degree of 90), nor the resolution or accuracy of global elastic thickness maps [see *Watts*, 2001, p 418] are of sufficient resolution to provide feedback on GOCE observations at ~100 km spatial scales (equivalent to harmonic degree of 200).
- 268

269 To our knowledge, there is currently no global crustal thickness model available of 270 sufficient resolution that would allow us to account for and model isostatic compensation 271 effects at or near the GOCE spatial resolution of ~100 km, without having to rely on 272 simplified hypotheses such as those behind the A/H or P/H models. Vening-Meinesz-type 273 models rely on the core assumption that local topographic loads are supported mechanically 274 by the lithosphere, so are very similar to the uncompensated topography (option 1 below) at 275 short spatial scales, and are not included here. The limited resolution of crustal thickness models (option 5 below) is exemplified in Sect. 4.2. In the absence of "observation-based" 276 277 crustal thickness models of sufficiently high spatial resolution, we are restricted to test the 278 following five modelling variants of Earth's topography and its isostatic compensation:

- 279 (1) uncompensated [rock-equivalent] topography, ice and oceans,
- 280 (2) A/H isostatic compensation plus the effect of (1),
- 281 (3) P/H isostatic compensation plus the effect of (1),
- 282

284

- 2 (4) A combination of A/H and P/H, that uses A/H over the continents and P/H over
- the oceans, plus the effect of (1),
 - (5) the Crust 2.0 lithosphere model.

Also because of the lack of a high-resolution 3D density model of the crust and lithosphere, we are unable to account for the isostatic compensation of mass anomalies.

287 **3.2 Rock-equivalent topography**

RET is a representation of Earth's topography that "compresses" ocean water and ice into layers equivalent to the mass-density of topographic rock (using the frequently presumed mean value of 2670 kg m⁻³), while keeping the water and ice masses constant. RET allows 291 computation of implied gravity effects based on a single constant uniform mass-density over292 land, ocean areas and ice shields.

For our topography-based GOCE GGM evaluation, RET is required in a spherical 293 294 The published version of DTM2006.0 [Pavlis et al., 2007; harmonic representation. 295 http://earth-info.nga.mil/GandG/wgs84/gravitymod/egm2008/first_release.html] cannot be 296 used directly because it describes the surface of the solid Earth above or below local mean 297 sea level. Over Greenland and Antarctica, DTM2006.0 heights are reckoned to the top of the 298 ice shields so the incorrect RET would be assigned to ice masses; likewise for the oceans. As 299 such, the scheme depicted in Fig. 1 is used to appropriately assign mass densities to ice and 300 ocean water. We have constructed a RET in the spatial domain that accounts for the effect of 301 the ocean water masses and ice shields over Greenland and Antarctica, and derived its 302 spherical harmonic coefficients. The construction, which we name RET2011, was based on 303 following three-step procedure.

304 First, a 5'×5' global grid of DTM2006.0 heights H^* to maximum degree $n_{max}^{DTM2006} =$ 305 2160 was computed using the spherical harmonic expansion [*EGM-Team*, 2008]

$$306 \qquad H^* = \sum_{n=0}^{n_{max}^{Datacool}} \sum_{m=0}^{n} (\overline{HC}_{nm} \cos m\lambda + \overline{HS}_{nm} \sin m\lambda) \overline{P}_{nm} (\cos \theta) \tag{1}$$

307 where \overline{HC}_{nm}^* and \overline{HS}_{nm}^* are the 4π -fully-normalized spherical harmonic coefficients of the 308 DTM2006.0 database, $\overline{P}_{nm}(\cos\theta)$ are the 4π -fully-normalized associated Legendre functions 309 of degree *n* and order *m*, and λ longitude and θ geocentric co-latitude of the computation 310 point.

311 Second, the grid of DTM2006.0 H^* was converted to RET elevations H by 312 transforming the ocean depths using [*Rummel et al.*, 1988; *Wieczorek*, 2007]

313
$$H = \begin{cases} H^*(1 - \rho_W / \rho) &, H^* < 0 \\ H^* &, H^* \ge 0 \end{cases}$$
(2)

where $\rho_{\rm W}$ is the mean mass-density of ocean water (1030 kg m⁻³) and ρ the mean massdensity of topographic rock (2670 kg m⁻³). This reduction of ocean depths by factor $(1 - \rho_{\rm W} / \rho) = 0.614$ compresses the ocean water into RET. Over Greenland and Antarctica DTM2006.0 heights represent the interface between ice and air, thus additional information on the bedrock underneath the ice shields is required to properly model the RET. Over these areas, DTM2006 was replaced by ETOPO1 (area-weight-averaged to a 5'×5' grid) which has been used to obtain RET heights through

321
$$H = H_{bed} + \Delta H_{ice}^{(-)} (1 - \frac{\rho_{ice}}{\rho}) + \Delta H_{ice}^{(+)} \frac{\rho_{ice}}{\rho}$$
(3)

where H_{bed} is the bedrock height, ρ_{ice} is the mean mass-density of ice (927 kg m⁻³) and $\Delta H_{ice}^{(+)}$ and $\Delta H_{ice}^{(-)}$ are the thicknesses of ice masses above and below mean sea level (MSL), cf. Fig 1. Equation (3) is valid for bedrock above MSL (e.g. $H_{bed} \ge 0$) and below MSL (e.g. $H_{bed} < 0$). The thickness $\Delta H_{ice}^{(+)}$ of ice masses above MSL are reduced by the factor $\rho_{ice} / \rho =$ 326 0.347 and the thickness $\Delta H_{ice}^{(-)}$ of ice masses below MSL are reduced by the factor 327 $(1 - \rho_{ice} / \rho) = 0.653.$







Fig. 1. Terrain types used to construct the rock-equivalent topography RET2011 heights.

Third, the 5' \times 5' grid of RET H was analyzed harmonically to yield spherical 332 harmonic coefficients HC_{nm} , HS_{nm} of RET2011. Though the GGM evaluation requires the 333 \overline{HC}_{nm} , \overline{HS}_{nm} coefficients only to degree 250, we derived \overline{HC}_{nm} , \overline{HS}_{nm} to degree 360 which 334 can be used for RET-based evaluation of future GGMs. Our spherical harmonic analysis is 335 336 based on least-squares estimation of the harmonic coefficients [e.g., Colombo, 1981; Torge 337 2001, p. 272]. Following this approach, a regular global grid of RET heights (symmetric to the equator) is used to develop grid elements along the same parallel into Fourier series in 338 $\sin m\lambda$ and $\cos m\lambda$. Based on the Fourier series coefficients the 4pi-fully normalized 339 spherical harmonic coefficients \overline{HC}_{nm} , \overline{HS}_{nm} are obtained through least-squares estimation. 340 RET2011 heights expanded to degree 250 (the maximum resolution of the second generation 341 342 GOCE models) are shown in Figure 2. 343



344

Fig. 2. Earth's rock-equivalent topography RET2011 to spherical harmonic degree 250.
Robinson projection, units in metres. Grey boxes show evaluation regional used in Sect. 4

347 **3.3 Potential coefficients**

348 3.3.1 Uncompensated RET

349 The \overline{HC}_{nm} , \overline{HS}_{nm} coefficients of RET2011 were converted into gravitational potential 350 spherical coefficients $\overline{C}_{nm}^{\text{RET}} \overline{S}_{nm}^{\text{RET}}$ using [*Rummel et al.*, 1988; *Kuhn and Featherstone*, 2003]: 351

$$352 \qquad \left\{ \overline{C}_{nm}^{RET} \atop \overline{S}_{nm}^{RET} \right\} = \frac{3}{2n+1} \cdot \frac{\rho}{\overline{\rho}} \left[\left\{ \overline{HC1}_{nm} \atop \overline{HS1}_{nm} \right\} + \frac{n+2}{2} \left\{ \overline{HC2}_{nm} \atop \overline{HS2}_{nm} \right\} + \frac{(n+2)(n+1)}{6} \left\{ \overline{HC3}_{nm} \atop \overline{HS3}_{nm} \right\} \right]$$
(4)

with $\overline{\rho}$ mean mass-density of Earth (5515 kg m⁻³) and ρ the mean mass-density of topographic rock (2670 kg m⁻³). $\overline{HC1}_{nm}$, $\overline{HS1}_{nm}$ are the spherical harmonic coefficients of the dimensionless surface function H1 := H / R and obtained from

356
$$\frac{\overline{HC1}_{nm} = \overline{HC}_{nm} / R}{\overline{HS1}_{nm} = \overline{HS}_{nm} / R},$$
(5)

357 where *R* is the equatorial Earth radius of 6378137 m [*Torge*, 2001]. $\overline{HC2}_{nm}$, $\overline{HS2}_{nm}$ denote 358 the spherical harmonic coefficients of surface function *H*2

359
$$H2 := \left(\frac{H}{R}\right)^2 = \sum_{n=0}^{360} \sum_{m=0}^n \left(\overline{HC2}_{nm} \cos m\lambda + \overline{HS2}_{nm} \sin m\lambda\right) \overline{P}_{nm}(\cos \theta)$$
(6)

360 and $\overline{HC3}_{nm}$, $\overline{HS3}_{nm}$ are the coefficients of surface function H3

361
$$H3 := \left(\frac{H}{R}\right)^{3} = \sum_{n=0}^{360} \sum_{m=0}^{n} (\overline{HC3}_{nm} \cos m\lambda + \overline{HS3}_{nm} \sin m\lambda) \overline{P}_{nm} (\cos \theta)$$
(7)

For evaluation of Eq. (4), $HC1_{nm}$, $HS1_{nm}$ are readily available from Eq. (5), while two additional spherical harmonic analyses are needed to derive the coefficients $\overline{HC2}_{nm}$, $\overline{HS2}_{nm}$ and $\overline{HC3}_{nm}$, $\overline{HS3}_{nm}$ of the surface functions H2 and H3, respectively. The surface functions H2 and H3 are computed as a function of H (Eqs. 6 and 7) after the H were synthesized on a high-resolution grid using

367
$$H = \sum_{n=0}^{360} \sum_{m=0}^{n} (\overline{HC}_{nm} \cos m\lambda + \overline{HS}_{nm} \sin m\lambda) \overline{P}_{nm} (\cos \theta)$$
(8)

368

Equation (4) is a series expansion to third-order of H, which is obtained by replacing 369 the inverse distance in Newton's integral through a series of Legendre polynomials [e.g., 370 Heiskanen and Moritz, 1967, p. 32]. A first-order expansion delivers well above 90% of the 371 372 overall topography-implied gravity signal [cf. Novák and Grafarend 2005, Fig. 3]. With any additional term, topography-implied signal captured by the $\overline{C}_{nm}^{RET} \overline{S}_{nm}^{RET}$ potential coefficients 373 comes closer to 100% and the contribution of every additional term is smaller than the 374 375 previous [Wieczorek, 2007]. According to Wieczorek [2007, Fig. 9 ibid.], the maximum (truncation) error of a third-order expansion is a few mGal, and the average root mean square 376

(RMS) error is well below the mGal-level. Given that the global RMS gravity signal strength
is ~35 mGal [*EGM-Team*, 2008], the third-order expansion appears sufficient.

379

380 3.3.2 Airy-Heiskanen compensation

381 In the A/H model, a lighter lithosphere is assumed to float on a denser mantle, and isostatic compensation is assumed to take place locally in vertical columns of equal mass-382 density [e.g., Heiskanen and Moritz, 1967; Watts, 2001, Torge, 2001]. As a consequence, the 383 384 depth of the sub-surface compensation mass is directly related to the height of the topography ("local compensation"), and the spatial resolution of the A/H compensation model is 385 [formally] identical to the resolution of the topographic model used. 386 The potential 387 coefficients of the A/H-compensated RET are computed from a series expansion to thirdorder [Rummel et al., 1988, Eq. 24] 388

$$\begin{cases}
\overline{C}_{nm}^{A/H} \\
\overline{S}_{nm}^{A/H}
\end{cases} = \frac{3}{2n+1} \cdot \frac{\rho}{\overline{\rho}} \left[\left[1 - \left(\frac{R-T}{R}\right)^n \right] \left\{ \overline{\frac{HC1}{HS1}}_{nm} \right\} + \frac{n+2}{2} \left[1 + \frac{\rho}{\rho_m - \rho} \left(\frac{R-T}{R}\right)^{n-3} \right] \left\{ \overline{\frac{HC2}{HS2}}_{nm} \right\} + \frac{(n+2)(n+1)}{6} \left[1 - \left(\frac{\rho}{\rho_m - \rho}\right)^2 \left(\frac{R-T}{R}\right)^{n-6} \right] \left\{ \overline{\frac{HC3}{HS3}}_{nm} \right\} \right] \tag{9}$$

where T denotes the mean depth of compensation and ρ_m the mass-density of the mantle. 390 Here we use T = 30 km and $\rho_m = 3270$ kg m⁻³ [Torge, 2001, p. 341]. The potential 391 coefficients $\overline{C}_{nm}^{A/H}$, $\overline{S}_{nm}^{A/H}$ contain the effect both of the topography and of the A/H-392 compensation masses. The practical computation of the $\overline{C}_{nm}^{A/H}$, $\overline{S}_{nm}^{A/H}$ is straightforward as the 393 required sets of potential coefficients of the uncompensated RET $(\overline{HC1}_{nm}, \overline{HS1}_{nm})$, 394 $\overline{HC2}_{nm}$, $\overline{HS2}_{nm}$ and $\overline{HC3}_{nm}$, $\overline{HS3}_{nm}$) are readily available from Sect. 3.3.1. We acknowledge 395 396 that the value of T = 30 km is not valid for oceans, so a combination is trialed later (Sect 397 3.3.4).

398

399 3.3.3 Pratt/Hayford compensation

400

401 The P/H isostatic compensation uses a constant depth of compensation along with 402 laterally-varying mass-densities of vertical columns [e.g., *Watts*, 2001, *Torge*, 2001]. A 403 compact formulation of the potential coefficients $\overline{C}_{nm}^{P/H} \overline{S}_{nm}^{P/H}$ of the P/H-compensated 404 topography is given by *Göttl and Rummel* [2009] as:

$$\left\{ \frac{\overline{C}_{nm}^{P/H}}{\overline{S}_{nm}^{P/H}} \right\} = \frac{3}{2n+1} \cdot \frac{\rho}{\overline{\rho}} \left[\left\{ \frac{\overline{hC1}_{nm}}{\overline{hS1}_{nm}} \right\} + \frac{n+2}{2} \left\{ \frac{\overline{hC2}_{nm}}{\overline{hS2}_{nm}} \right\} \frac{(n+2)(n+1)}{6} \left\{ \frac{\overline{hC3}_{nm}}{\overline{hS3}_{nm}} \right\} \right] + \frac{3}{(2n+1)(n+3)} \frac{\rho}{\overline{\rho}} \left[1 - \left(\frac{R-D}{R} \right)^{n+3} \right] \left\{ \frac{\overline{\rho}\overline{C}_{nm}}{\overline{\rho}S_{nm}} \right\}$$
(10)

406 where *D* is the depth of compensation [here 100 km], $\overline{\rho}$ mean mass-density of Earth (5515 407 kg m⁻³), ρ the mean mass-density of topographic rock (2670 kg m⁻³). The $\overline{hC1}_{nm}$, $\overline{hS1}_{nm}$, 408 $\overline{hC2}_{nm}$, $\overline{hS2}_{nm}$, and $\overline{hC3}_{nm}$, $\overline{hS3}_{nm}$ are the spherical harmonic coefficients of the 409 dimensionless height function h/R times the dimensionless density function ρ_i / ρ and 410 $\overline{\rho C}_{nm}$, $\overline{\rho S}_{nm}$ are the spherical harmonic coefficients of the dimensionless density function 411 ρ_i / ρ [*Mladek*, 2006, p 74]:

412

413
$$h1 := \left(\frac{h}{R}\frac{\rho_i}{\rho}\right) = \sum_{n=0}^{360} \sum_{m=0}^{n} \left(\overline{hC1}_{nm} \cos m\lambda + \overline{hS1}_{nm} \sin m\lambda\right) \overline{P}_{nm}(\cos\theta)$$
(11)

414
$$h2 := \left(\frac{h}{R}\frac{\rho_i}{\rho}\right)^2 = \sum_{n=0}^{360} \sum_{m=0}^n \left(\overline{hC2}_{nm} \cos m\lambda + \overline{hS2}_{nm} \sin m\lambda\right) \overline{P}_{nm}(\cos\theta)$$
(12)

415
$$h3 \coloneqq \left(\frac{h}{R}\frac{\rho_i}{\rho}\right)^3 = \sum_{n=0}^{360} \sum_{m=0}^n (\overline{hC3}_{nm} \cos m\lambda + \overline{hS3}_{nm} \sin m\lambda) \overline{P}_{nm}(\cos \theta)$$
(13)

416

417
$$\rho_1 := \frac{\rho_i}{\rho} = \sum_{n=0}^{360} \sum_{m=0}^n (\overline{\rho C}_{nm} \cos m\lambda + \overline{\rho S}_{nm} \sin m\lambda) \overline{P}_{nm} (\cos \theta)$$
(14)

418

419 Variable *h* denotes the equivalent rock heights of the P/H model and ρ_i are the [individual] 420 mass-densities of the vertical columns. According to *Göttl and Rummel* [2009] the P/H 421 equivalent rock heights *h* are determined via: 422

423
$$h = \begin{cases} H , H^* \ge 0 \\ \left(\frac{\rho(R+H^*)^3[-R^3+(R-D)^3]-\rho_W(R-D)^3[-R^3+(R+H^*)^3]}{\rho_W[R^3-(R+H^*)^3]-\rho[R^3-(R-D)^3]}\right)^{1/3} - R , H^* < 0 \end{cases}$$
(15)

where *H* are the RET2011 heights [from Eqs.(2) and (3)], H^* are the DTM2006 bathymetric depths/topographic heights, and ρ_W is the mean mass-density of ocean water (1030 kg m⁻³). Equation (15) is the formulation of the P/H equilibrium condition over the oceans [*Göttl and Rummel* 2009, p 1253]. Over land areas, RET2011 heights *H* (topography or ice) and *h* are identical, while *H* and *h* are different over the oceans. Note that *Göttl and Rummel* [2009] used a different sign convention for bathmetric depths. The individual mass-densities ρ_i are obtained from

431
$$\rho_i = \rho \left(\frac{R^3 - (R - D)^3}{(R + h)^3 - (R - D)^3} \right)$$
 (16)

For the practical computation of the P/H-compensated rock-equivalent topography, we backconverted the RET2011 heights to bathymetric depths H^* over the oceans, and applied Eq.

434 (15) to obtain rock-equivalent heights h, consistent with the P/H equilibrium condition. We

- 435 then computed the individual mass-densities P_i [Eq. (16)] of the 5' \times 5' grid, and analyzed 436 harmonically the dimensionless linear, squared and cubic height functions h1, h2, h3 [Eq. 437 (11)-(13)]. A further harmonic analysis of the 5' \times 5' grid of ρ 1 [Eq. (14)] yielded the $\overline{\rho C}_{nm}$, $\overline{\rho S}_{nm}$ coefficients required to finally obtain the $\overline{C}_{nm}^{P/H} \overline{S}_{nm}^{P/H}$ potential coefficients of the 438 P/H compensated rock-equivalent topography [Eq. (10)]. The potential coefficients $\overline{C}_{nm}^{P/H}$, 439 $\overline{S}_{nm}^{P/H}$ contain the effect both of the topography and of the P/H-compensation masses.
- 440
- 441

442 **3.3.4** Combined A/H and P/H compensation model

443 Göttl and Rummel [2009] analyzed A/H and P/H compensated gravity anomalies over land 444 and ocean areas and found that the A/H is better suited than P/H to model the isostatic 445 compensation of large mountain chains, while their analysis suggests that P/H is a better approximate description of isostasy over deep ocean trenches. We therefore combine the 446 447 classical A/H [Sect. 3.3.2] and P/H [Sect. 3.3.3] hypotheses, by using A/H over land areas 448 and P/H over the oceans. A/H and P/H are combined in the spatial domain by using gravity implied by the P/H-compensated topography at points where $H^* < 0$ and the A/H-449 compensated topography elsewhere, see also Wild and Heck [2005]; Makhloof [2007] who 450 451 used the same combination strategy. "By this mixture, one of the drawbacks of the original 452 Airy-Heiskanen model - the fact that the antiroots may rise above the ocean bottom in deep 453 sea trough areas – can be avoided." [Wild and Heck 2005, p233].

454

455 **3.4 Gravity computations**

Gravity disturbances δg^{GGM} from each GGM were computed at points specified by radius *r*, 456 longitude λ and geocentric co-latitude θ from the spherical harmonic coefficients 457 \overline{C}_{nm}^{GGM} \overline{S}_{nm}^{GGM} of the various GOCE GGMs via [*Heiskanen and Moritz*, 1967; *Torge*, 2001] 458

$$459 \qquad \delta g^{GGM} = \frac{GM^{GGM}}{r^2} \sum_{n=n_1}^{n_2} \left(\frac{a^{GGM}}{r}\right)^n (n+1) \sum_{m=0}^n (\overline{C}_{nm}^{GGM} \cos m\lambda + \overline{S}_{nm}^{GGM} \sin m\lambda) \overline{P}_{nm}(\cos \theta) \tag{17}$$

where a_{GGM} (model scale factor) and GM_{GGM} (gravitational constant times Earth's mass) are 460 the model-specific constants, and n_1 , n_2 are the minimum and maximum harmonic degree, 461 respectively, of the spectral band being examined. Similarly, the RET potential coefficients 462 $\overline{C}_{nm}^{RET} \overline{S}_{nm}^{RET}$ are evaluated to give gravity disturbances δg^{RET} implied by the uncompensated 463 464 RET.

$$465 \qquad \delta g^{RET} = \frac{GM}{r^2} \sum_{n=n_1}^{n_2} \left(\frac{a}{r}\right)^n (n+1) \sum_{m=0}^n (\overline{C}_{nm}^{RET} \cos m\lambda + \overline{S}_{nm}^{RET} \sin m\lambda) \overline{P}_{nm}(\cos \theta) \tag{18}$$

where $GM = GM^{GGM} = 3.986004415 \times 10^{14} \text{ m}^3 \text{ s}^{-2}$ for all seven GGMs assessed (Table 1). 466 Accordingly, evaluating Eq. (18) with the $\overline{C}_{nm}^{A/H} \overline{S}_{nm}^{A/H} (\overline{C}_{nm}^{P/H} \overline{S}_{nm}^{P/H})$ gives gravity disturbances 467 $\delta g^{A/H}$ ($\delta g^{P/H}$) of the A/H-compensated and P/H-compensated topography, respectively. The 468 gravity $\delta g^{A/H-P/H}$ implied by the combined A/H-P/H model is obtained by using $\delta g^{P/H}$ over 469

470 the oceans and $\delta g^{A/H}$ elsewhere. Hereafter, we use the general term "gravity" for δg^{GGM} , 471 δg^{RET} and $\delta g^{A/H}$, $\delta g^{P/H}$ and $\delta g^{A/H-P/H}$ from Eqs. (17) and (18).

Equations (17) and (18) were evaluated with the harmonic_synth software [*Holmes* and Pavlis, 2008] on the surface of an authalic sphere with radius r = R = 6378137 m. This sets the attenuation factor $(a/r)^n$ in Eq. (18) to unity, while $(a^{GGM}/R)^n$ is very close to unity in Eq. (17). The $(a^{GGM}/r)^n$ ranges between 0.999973 and 1, because $a^{GGM} - r < 1$ m for all seven GGMs assessed and the smallest possible value of $(a^{GGM}/r)^n$ is 0.999973 (for *n* = 250 and $a^{GGM} = 6378136.3$ m). As a consequence, the attenuation factors only affect our evaluation results by less than 0.003%, which is negligible.

479

480 **4. Analyses and results**

481 **4.1 Evaluation criteria**

482 **4.1.1 Correlation coefficients and reduction rates**

We computed $10' \times 10'$ grids of GGM gravity for each GGM in Table 1 over a series of twodegree spectral bands [n, n+1], starting from [2, 3] up to $[n_{max}-1, n_{max}]$ the model's maximum degree n_{max} , and then compared these against gravity implied by the (i) uncompensated RET, (ii) A/H-compensated RET, (iii) P/H-compensated RET and (iv) A/H-P/H combined compensated RET in the same bands in the spatial domain.

488 To evaluate the GGM's spectral content as a function of degree we use cross-489 correlation coefficients (CCs) between δg^{GGM} and δg^{RET} , δg^{GGM} and $\delta g^{A/H}$, δg^{GGM} and 490 $\delta g^{P/H}$, and δg^{GGM} and $\delta g^{A/H-P/H}$, respectively. CCs between topography and gravity have 491 been used previously, e.g., by *Rapp* [1982], *Rummel et al.*, [1988] and *Wieczorek* [2007], 492 amongst many others. We also use a new indicator called reduction rates (RRs), given by:

493
$$RR = 100\% \cdot \left(1 - \frac{RMS(\delta g^{REF} - \delta g^{GGM})}{RMS(\delta g^{REF})}\right)$$
(19)

494 where RMS is the root mean square of the δg^{REF} and the differences ($\delta g^{REF} - \delta g^{GGM}$), 495 respectively, and δg^{REF} is the reference signal, which can either be gravity implied by the 496 uncompensated topography (δg^{RET}),by the A/H-compensated topography ($\delta g^{A/H}$),the P/H-497 compensated topography ($\delta g^{P/H}$), or the combined A/H-P/H-compensated topography 498 $\delta g^{A/H-P/H}$.

Reduction rates (RRs) quantify the extent to which the signal strength of δg^{REF} is 499 reduced ('explained') by the model gravity δg^{GGM} or, in other words, the strength of δg^{REF} 500 501 signals captured by the δg^{GGM} . Moderate positive RRs (say about 30% to 50%) indicate considerable topography-generated gravity signals are captured by the GGM, whereas RRs 502 503 near or below 0% show that the GGM signal is unrelated to the topography. Smaller, but 504 positive, RRs (say about 10% to 20%) indicate that the GOCE model contains TIG signals δg^{REF} to some, but limited, extent. RRs close to 80-90 % indicate that the GGM signal is 505 almost entirely generated by the modeled topography. However, given the presence of 506

unmodeled mass-density anomalies in the real topography and the Earth's interior, such
values do not occur at the spatial scales resolved by GOCE (see Sects 4.2 and 4.3). From Eq.
(19), RRs cannot exceed 100%.

Moderate positive RRs always correspond to large positive CCs between δg^{REF} and 510 δg^{GGM} . Conversely, a large positive CC between δg^{REF} and δg^{GGM} does not necessarily 511 correspond to a large RR. In cases where the model is underpowered near the model 512 resolution (due to gravity attenuation at satellite height), we consider it possible that δg^{REF} 513 and δg^{GGM} are strongly correlated (the gravity highs and lows appear at the same locations), 514 but the δg^{GGM} RMS signal strength is smaller than implied by the topography δg^{REF} . 515 Despite larger CCs, RRs will then be low, thus better indicating the deteriorating quality of 516 the model. We have tested RRs extensively using both the δg^{RET} , $\delta g^{A/H}$, $\delta g^{P/H}$ and 517 $\delta g^{A/H-P/H}$ as reference δg^{REF} in Eq. (19). As a prerequisite for moderate positive RRs, the 518 RMS signal strength of δg^{REF} has to be similar (or larger) than that of the observed gravity 519 δg^{GGM} . Otherwise, the RMS ($\delta g^{REF} - \delta g^{GGM}$) will exceed the RMS(δg^{REF}), failing to 520 indicate topography-generated signals in the GGM. 521

522

523 **4.1.2 Effective and formal model resolution**

524 Degree-wise comparisons between quantities derived from spherical harmonic models are always subject to oscillations [e.g., Rapp, 1982; Rummel et al., 1988; Wieczorek, 2007; 525 Gruber et al., 2011]. Because these oscillations also propagate into quality indicators (be it 526 527 CCs, RRs or other indicators), and because most of the GGMs contain topographic signals 528 over their entire spectrum, it is generally difficult to discriminate the maximum harmonic 529 degree upon which the GGMs deliver full (i.e., not affected by attenuation) information on Earth's gravity field (also see Gruber et al., [2011]; Hirt et al., [2011]). We found that 530 531 neither the harmonic degree where the RRs are maximum nor constant thresholds (e.g., 20 %) 532 are informative numerical criteria because these oscillations vary from region to region. As a 533 compromise, we use the following simple numerical threshold

534
$$t = f \times r$$
,

(20)

where f = 0.85 and \overline{r} is the GGMs average RR in band 100 to 175 over the region under investigation.

537 What we will term the *effective resolution* is the smallest harmonic degree (but larger 538 than 150) where the GGM's RR falls below our threshold criterion (Eq. 20). The effective 539 resolution indicates the degree where the GGMs seem to possess almost full spectral power. 540 Opposed to this, the *formal resolution* is the maximum expansion degree of the GGMs in 541 Table 1. We acknowledge that the criterion in Eq. (20) is somewhat arbitrary because the 542 choice of factor f influences the threshold and thus the interpreted effective resolution. 543 However, the use of this criterion suppresses the influence of the oscillations (Sections 4.2 544 and 4.3) on the choice of effective resolution because the same criterion applies to all GGMs 545 and they are being compared in a relative manner.

546

547 **4.2 Preliminary comparisons**

548 To initially analyze the spectral properties of our data sets, we have computed 549 [dimensionless] potential degree variances σ_n [e.g., *Rapp*, 1982; *Rummel et al.*, 1988]

550
$$\sigma_n = \sum_{m=1}^m \overline{C}_{nm}^2 + \overline{S}_{nm}^2$$
 (21)

where *n* is the degree, *m* the order and $\overline{C}_{nm} \overline{S}_{nm}$ are the spherical harmonic coefficients of the 551 GGMs, of the uncompensated RET, or of the A/H- or P/H-compensated topography. From 552 553 Fig. 3, the (uncompensated) RET significantly exceeds the spectral power of Earth's 554 observed gravity field, as represented through EGM2008 and GOCE-TIM3. This behavior 555 (e.g., Rummel et al. [1988, Fig. 2]; Watts, [2001, p 416]) shows that the gravitational attraction of isostatic compensation masses and other mass-density anomalies in the Earth's 556 557 interior "compete" with the attraction of Earth's uncompensated topography, most significantly at long- and medium wavelengths. The A/H compensation model diminishes 558 559 the spectral power of the uncompensated topography to a level well below that of Earth's 560 observed gravity field (see also Rummel et al. [1988]). Opposed to this, the spectral power of 561 the P/H-compensated topography is very similar to that of Earth's observed gravity field, 562 which is in agreement with Makhloof [2007, p102].

563





Fig. 3. Dimensionless degree variances of selected GGMs and topographic/isostatic models.

567 To gain some insight into the effectiveness of our topography and compensation 568 variants to indicate topography/isostasy-implied signals in the GOCE gravity fields, we 569 compared gravity δg^{GGM} from the highest-resolution space-collected GGM GOCE-TIM3 570 with δg^{RET} , $\delta g^{A/H}$ and $\delta g^{P/H}$, and with the combined $\delta g^{AH/PH}$ as a function of the

- 571 spherical harmonic degree over a near-global area (-83.3°≤ ϕ ≤83.3° and -180° ≤ λ ≤ 180°).
- 572 From Fig. 4 (top), RRs using the uncompensated RET2011 as a reference are generally larger
- 573 than RRs using compensated RET. RRs using $\delta g^{P/H}$ as a reference are largest at the long
- 574 spatial scales, at the 20% level at medium scales and comparable to that of RET2011 beyond
- 575 degree 200. From Fig. 4 (top), P/H appears to better describe isostasy globally at long- and
- 576 medium scales than A/H. For the combined A/H-P/H model, RRs are larger than of A/H and
- 577 below those of the P/H.



578

579 **Fig. 4.** Reduction rates (top) and cross-correlation coefficients (bottom) between GOCE-580 TIM3 and various topographic/isostatic models as a function of harmonic degree n. 581 Evaluation area is $-83.3^{\circ} \le \varphi \le 83.3^{\circ}$ and $-180^{\circ} \le \lambda \le 180^{\circ}$.

582 The CCs for all three topographic/isostatic models agree reasonably well over all 583 harmonic degrees (Fig. 4 bottom), and thus do not allow discrimination between the different Only RRs are capable of discriminating between the 584 topographic/isostatic models. 585 topographic/isostatic models (Fig. 4 top), and additionally indicate the increasing relevance of topography-generated signals in the observed gravity field (seen by the steadily increasing 586 RRs up to degree ~200). Given that RRs require a reference signal δg^{REF} of sufficient 587 spectral power (see Sect. 4.1.1 and Fig. 3), it becomes clear that the underpowered A/H 588 589 compensated topography does not serve well as reference signal at long and medium spatial 590 scales (seen by the very low or negative RRs for A/H in Fig. 4 top). Focusing on spatial 591 scales less than ~100 km (that is, beyond harmonic degree 200), CCs and RRs indicate -592 irrespective of using uncompensated or compensated topography – a declining amount of topography-generated gravity signals. However, neither the CCs nor RRs indicate that the 593 594 agreement of GOCE-measured gravity with Earth's topography improves over RET2011 595 when employing the isostatic compensation models at ~100 km spatial scales.

Neglecting the isostatic compensation masses, the uncompensated RET2011 should theoretically be the poorer representation of Earth's topography/isostasy, while adding isostatic compensation effects to RET2011 should be a theoretically better representation. However, the observation that the isostatic models do not improve the agreement over RET2011-only at medium and short spatial scales suggests that none of the isostatic models included here is a very suitable representation of compensating masses.

For comparison purposes, the Crust.2.0 lithosphere model has been tested as an 602 603 "observation-based" global description of crustal thickness (potential coefficients are from 604 Kuhn and Featherstone, [2003], derived through spherical harmonic analysis of the upper-605 middle and lower crustal layers as well as the crust-mantle boundary aka Moho). From Fig. 606 3, Crust 2.0's spectral power ranges between RET and Earth's observed gravity up to harmonic degree ~50, and declines rapidly at medium wavelengths. Comparison among 607 608 Crust 2.0-implied gravity and the GOCE-observed gravity field (Fig. 4) shows generally low 609 CCs (less than +0.5), with the RRs indicating some crustal signals captured by GOCE (through GPS-based orbit determination) between degrees 10 and 40. The Crust.2.0-implied 610 611 gravity field bears little resemblance to the Earth's gravity field, and fails to deliver 612 meaningful information beyond degree ~40, so is unusable to provide a feedback on the GOCE-measured short-scale gravity field. 613

We acknowledge that the A/H and P/H isostatic compensation models reduce the differences between Earth's observed gravity field and gravity effects implied by the uncompensated topography regionally to some extent (cf. *Watts* [2011], Fig. 1; *Göttl and Rummel* [2009], p 1255). However, From Fig. 4 it is evident that the A/H and P/H models – along with the evaluation methodology applied here – fail to improve the agreement between GOCE and the uncompensated topography globally.

The observation that the A/H and P/H compensation models do not improve the agreement does not necessarily imply that isostatic compensation is not present at all at short, say ~100 km, scales. It only implies that the classical hypotheses are of limited use to accurately model local isostatic compensation globally. We conclude that the A/H and P/H and combined compensation models are not better suited than the uncompensated topography 625 (RET2011) to study the resolution of the new GOCE gravity fields. As a consequence, we 626 use the uncompensated topography δg^{RET} as reference δg^{REF} in our global and regional 627 comparisons in the sequel.

628

629 4.3 Near-global comparisons with RET2011

630 The polar regions ($|\phi| > 83.3^{\circ}$) that GOCE cannot fly over due to its orbital inclination 631 of 96.7° are excluded from the following comparisons. Figure 5 shows the RRs (top) and CCs (bottom) between 10'×10' near-global grids of δg^{GGM} and δg^{RET} as a function of degree 632 for each GGM (cf. Table 1). RRs increase to ~35% up to degree ~150, almost identically for 633 634 all models, showing the increasing strength of topographic gravitational signals captured by 635 the GGMs. Up to degree ~150, neither the CCs nor RRs differ markedly for any of the GGMs. Hence, at low- and medium-frequencies, both indicators are unable to discriminate 636 637 among their performance.

Beyond degree ~150, RRs and CCs start to diverge for all GGMs. This now allows 638 639 for discrimination among their short-scale agreement with topography-generated gravity 640 signals. The topography is considered to be the dominant source of short-scale gravity field 641 signals [e.g., Forsberg and Tscherning, 1981; Pavlis et al., 2007; Hirt et al., 2010b, 2011], 642 which is why an improved agreement between measured and topography-generated gravity 643 can be expected with increasing harmonic degree n. Therefore, the drop in RRs and CCs 644 (Fig. 5) indicate that the GGMs lose spectral power, i.e., are increasingly unable to capture 645 the topography-implied gravity signal. From Fig. 5, we infer

- ITG-GRACE2010s starts losing topography-generated signals near degree ~160,
- All GOCE-GGMs capture topographic signals well up to degree ~175, with RRs close to ~40% and CCs near +0.75,
- The first-generation GOCE-GGMs SPW1 and TIM1 show a very similar decline in signal between degrees ~180 and ~200, whilst the second- and third-generation GOCE GGMs start losing topography signals between degrees ~200 and ~220.
- 652
- 653 Furthermore,
- The performance curves of DIR2 and TIM2, and of DIR3 and TIM3 are very close together, separated from SPW2 by a spectral difference of ~15 harmonic degrees.
- The third-generation DIR3 and TIM3 improve over the second generation DIR2 and TIM2 in the spectral band of ~200 to ~240, where the RRs of the third-generation models are by ~5 % larger than of those of the second generation. TIM3 shows the best agreement with gravity generated by the uncompensated topography.
- Even near or at their formal resolution (cf. Table 1), the GOCE GGMs exhibit
 positive RRs, showing the sensitivity of GOCE for short-scale topography signals,
 beyond degree ~200, albeit strongly attenuated. The highest sensitivity for short-scale
 gravity recovery is visible for DIR3 and TIM3 (positive RRs up to degrees ~240-250).
- DIR1 shows a good agreement with the topography up to its formal resolution of degree 240, but this is because of its high-frequency augmentation with terrestrial data (Table 1).



667

Fig. 5. Reduction rates and cross-correlation coefficients between RET2011 and GGM gravity as a function of degree n. Evaluation area is $-83.3^{\circ} \le \varphi \le 83.3^{\circ}$ and $-180^{\circ} \le \lambda \le 180^{\circ}$.

The effective GGM resolutions, computed from the criterion in Eq. (20), are reported in Table 2. TIM1 and SPW1 seem to capture most of the topography-generated gravity signals to degree ~195, which is somewhat larger than assessments based on ground-truth 674 gravity field functionals [cf. Gruber et al., 2011, Hirt et al., 2011]. The second- and third-675 generation GOCE GGMs possess almost full power to degree ~200 and ~220 respectively, which is an improvement over the first-generation GOCE GGMs and over ITG-676 677 GRACE2010s from the pre-GOCE-era. From Fig. 3, the GOCE TIM3 and EGM2008 degree 678 variances are in close agreement up to degree $\sim 210-220$, which corroborates our results from 679 Fig. 5. It should be stressed here that the GGMs spectral content extends beyond their 680 effective resolution; however, gravity field signals are found to be increasingly attenuated. 681 This is within expectation, given that satellite gravimetry cannot sense the high-frequency 682 gravity field because of the decaying gravity signals at satellite altitude [e.g., Kaula, 1966].

683 The relation between GOCE- and topography-implied gravity (Fig. 5) poses the 684 question why CCs are not greater than $\sim+0.7$, and only about $\sim35\%$ of GOCE-measured gravity is explained by RET at scales of ~100 km (regionally, these values can be higher, see 685 Section 4.2). Wieczorek [2007] analyzed the correlation between gravity (from a GRACE-686 687 based GGM) and (rock-equivalent) topography, yielding CCs at a similar level of +0.7, 688 which corroborates our results using RET2011. Importantly, CCs are not higher when 689 applying Crust 2.0, or A/H and P/H compensation models, as was shown in Fig. 4. We 690 therefore infer that topography-implied gravity (as well as those implied by the hypothesis-691 based compensated topography, cf. Sect 4.1) globally explains GOCE-captured gravity to 692 some, but still limited, extent at spatial scales of ~100 km, and significant crustal mass-693 density anomalies exist that superimpose the RET2011-generated signals, and those of the 694 A/H and P/H-compensated topography. Given that the topography/isostasy models used here 695 fail to explain the majority of GOCE-captured gravity signals, there is some potential to 696 derive better-resolution models of the lithosphere from GOCE (see the discussion in Section 697 5).

As a further justification for using RRs for GOCE-GGM assessment over CCs, the comparison between the two indicators in Fig 3 shows that CCs are less sensitive to indicate the extent of captured topography signals (seen by the almost constant correlation of +0.7 between degrees ~25 to ~150, while RRs steadily increase) and signal loss (CCs range between +0.1 and +0.5, while RRs are equally near 0%). Hence, only the correlation between model and topography-implied gravity cannot be recommended as a sole indicator for GGM analysis.

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706 **4.4 Regional comparisons with RET2011**

707 Figure 6 shows the differences between TIM2 and EGM2008 gravity in the same 708 spectral band of degrees 2 to 200. The agreement is satisfactory over wide parts of the 709 oceans, Europe, North America and Australia (areas where EGM2008 is partially based on 710 dense altimetric and terrestrial gravity data), while large differences are present over parts of 711 Asia, Africa, South America and Antarctica [see also Hirt et al., 2011; Pail et al., 2011; 712 Rummel et al., 2011]. These are regions of rather poor terrestrial gravity availability, and 713 where GOCE is expected to add significantly to gravity field knowledge. It was argued by 714 Hirt et al. [2011]: "Large differences, occurring over [these] regions [...], indicate GOCE may improve over EGM2008. However, since there are no ground truth data in these 715 716 regions, it is only possible to make an inference".

717

718	Table 2. Effective spherical harmonic degree for each GGM (cf. Table 1) as inferred by Eq.
719	(20).

Model	World ^a	Himalayas ^b	Andes ^c	Africa ^d	New	Antarctica ^f
					Guinea ^e	
ITG-Grace2010s	168	172	168	168	166	164
GOCE-SPW2	196	196	180	190	180	196
GOCE-SPW1	196	190	180	176	184	164
GOCE-DIR3	220	200	180	200	196	202
GOCE-DIR2	202	198	180	176	188	190
GOCE-DIR1	n/o	n/o	224	n/o	196	222
GOCE-TIM3	222	208	190	186	200	222
GOCE-TIM2	202	200	190	186	196	202
GOCE-TIM1	196	172	180	176	188	164

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721 $a \ \textbf{-83.3^{\circ}} \leq \phi \leq \textbf{83.3^{\circ}}, \ \textbf{-180^{\circ}} \leq \textbf{\lambda} \leq \textbf{180^{\circ}}$ c $-80^{\circ} \le \phi \le -60^{\circ}$, $-40^{\circ} \le \lambda \le 10^{\circ}$

n/o = not observed

 $e \ \text{-}10^{\circ} \text{\leq} \ \phi \text{\leq} \ 0^{\circ}, \quad 130^{\circ} \text{\leq} \lambda \text{\leq} \ 150^{\circ}$

b $20^{\circ} \le \phi \le 45^{\circ}$, $65^{\circ} \le \lambda \le 110^{\circ}$

d -30°≤ ϕ ≤ 30°, 10°≤ λ ≤ 40°

f -83.3°
< $\phi \leq$ -70.0°, -180°
<lash 180°

120° 180° 240° 300° 60° 0° 0° 90 60 60° 30° 30° 0° 0° ١, -30° -30° –60° -60 -90° 90 0° 0° 120° 180° 240° 60° 300° -5 0 5 10 -15 -10 15 20 -20

Fig. 6. Differences between gravity from EGM2008 and GOCE-TIM2, spectral band 2 to 728 200, Robinson projection, units in mGal. 729

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Fig. 7. Reduction rates and cross-correlation coefficients between RET2011 and GGM gravity as a function of degree n for five regional study areas: A: Himalaya $(20^{\circ} \le \varphi \le 45^{\circ})$ and $65^{\circ} \le \lambda \le 110^{\circ}$, B: Andes $(-40^{\circ} \le \varphi \le 10^{\circ})$ and $-80^{\circ} \le \lambda \le -60^{\circ}$, C: Africa $(-30^{\circ} \le \varphi \le 30^{\circ})$ and $10^{\circ} \le \lambda \le 40^{\circ}$, D: Papua New Guinea (PNG) $(-10^{\circ} \le \varphi \le 0^{\circ})$ and $130^{\circ} \le \lambda \le 150^{\circ}$), E: Antarctic (- $83.3^{\circ} \le \varphi \le -70.0^{\circ}$ and $-180^{\circ} \le \lambda \le 180^{\circ}$); the legend for all panels is shown in the bottom right.

Over the regions in Fig 7, we benchmark GOCE improvements by means of topography-implied gravity with data extending over the entire areas for the first time. Our evaluation offers some compromise in the interim until terrestrial/airborne gravimetry can be collected to provide real ground-truth, or the proprietary data sets [cf. *Pavlis et al.*, 2008] are declassified. We have chosen five regions of relatively poor ground gravity coverage – the 743 Himalayas, Andes, Africa, Papua New Guinea and Antarctica (North of the -83.3° parallel) which are marked in Fig. 2. Over each of these regions, RRs (and for the sake of 744 completeness CCs) are shown in Fig. 7. The effective degrees computed from Eq. (20) are 745 746 reported in Table 2. In comparison with Fig. 5, oscillations of the indicators are stronger, 747 which is due to the limited extent of the test regions. Over all regions, the comparisons 748 between the GOCE GGMs and topography-implied gravity show unanimously that

- 749 the second (third) generation GOCE gravity values are in close agreement with 750 topography-implied gravity up to degree ~ 200 (~ 220),
- 751
- 752
- 753 • GOCE delivers improved gravity field knowledge in band ~165 to ~200 compared 754 with GRACE.

• the second-generation of GOCE models improves upon the first generation in band

755 Over all regions, the GOCE-TIM2 (TIM3) solution appears to offer the best performance, 756 marginally better than GOCE-DIR2 (DIR3) and notably better than GOCE-SPW2 at short 757 scales. The agreement between topography and DIR1 reflects that it incorporates altimetry and terrestrial gravity data (and, most likely, topography information) in the high spectral 758 759 degrees. Over the rugged Himalava and Papua New Guinea areas, RRs are close to ~50 %, 760 indicating that the topography is a dominant source of the gravity field over these areas. Over 761 all of our test regions, GOCE-TIM3 captures RET-implied signals even in harmonic band 762 240 to 250, which follows from the slightly positive RRs, or, in other words, from the simple 763 observation that subtracting GOCE-TIM3 from RET-implied gravity reduces the RMS-signal strength of the latter [cf. Eq. (19)]. This behavior demonstrates that 12 months satellite 764 765 gravimetry observations capture information on Earth's gravity field in attenuated form down 766 to ~80 km spatial scales.

767

768 **5.** Discussion and Conclusions

~185 to ~200, and

769 Degree-wise comparisons between GOCE and gravity implied by Earth's topography 770 show that the second- and third-generation GOCE GGMs add significantly to Earth gravity 771 field knowledge over the Himalayas, Andes, Africa, Papua New Guinea and Antarctica, 772 regions with poor or classified ground gravity coverage and where conventional GGM 773 evaluation can be difficult.

774 Comparisons were made among eight official ESA GOCE models, based on $\sim 2, \sim 8$ 775 and ~12 months of space gravimetry observations. These first, second and third-generation 776 GOCE models gradually improve over ITG-GRACE2010s from the pre-GOCE-era, with the 777 third-generation GOCE GGMs enhancing our gravity field knowledge from harmonic degree 778 ~165 to ~200-220, or from spatial scales of ~120 km down to ~90-100 km, both globally and 779 regionally.

780 Our comparisons provide some feedback on ESA's three current GOCE gravity recovery philosophies: direct (DIR), time-wise (TIM) and space-wise (SPW), and on the 781 782 effective model resolution, indicating the highest degree where they seem to possess almost 783 full spectral power. Based on second-generation comparisons, the TIM and DIR approaches 784 offer a better agreement with topography-implied signals than the SPW approach. Both for 785 the second- and third generation models, the TIM and DIR approaches showed similarly

close agreement with topography-implied gravity, and the third-generation GOCE models
were found to capture most of topography-generated gravity field signal to spherical
harmonic degrees of ~200-220.

Despite being theoretically a poorer description of the Earth's uppermost mass distribution, the uncompensated topography turned out to be a data source that seems suitable for providing feedback on GOCE gravity field models. The spatial resolution of current lithosphere models based on observations (from seismic refraction data or elastic thicknesses estimates) is not fine enough to provide a feedback on the GOCE gravity models everywhere on Earth.

Therefore, in the absence of better strategies, isostasy was tested based on the classical though simplistic models of Airy/Heiskanen and Pratt/Hayford, and a hybrid combination of them, because these hypotheses [formally] offer a spatial resolution commensurate with GOCE. However, failing to confer improvements over the agreement seen among GOCE and the uncompensated topography, the isostasy models tested here – specifically the A/H hypothesis – are of limited benefit to precisely describe isostasy globally at the spatial scales resolved by GOCE.

802 In the absence of an efficient high-resolution description of isostasy, the new GOCE 803 gravity field models may become an important new data source that implicitly contain 804 information on yet unknown mass-density features [cf. Benedek and Papp, 2009; Braitenberg 805 et al., 2010]. In modeling the density structure of the lithosphere, the GOCE models may 806 serve as important boundary condition [cf. Marotta, 2003]. The use of GOCE gravity 807 observations specifically for improved recovery of crustal thicknesses (Moho recovery) has 808 been proposed or is under investigation [e.g., Braitenberg et al., 2010; Tedla et al., 2010; 809 Bagherbandi, 2011; Köther et al., 2011; Reguzzoni and Sampietro 2012].

810 The third-generation GOCE models resolve the Earth's gravity field at spatial scales 811 not recovered before by other space gravimetry missions. Showing the closest agreement 812 with topography-implied signals, the TIM3 and DIR3 models are recommended as "currently 813 the best" medium-wavelength space-collected data sources to describe the gravity field over 814 some regions. Further improvements should be anticipated from future GOCE model 815 generations that are based on data volumes larger than ~12 months.

At spatial scales as short as ~80-90 km (harmonic degrees of 220 to 250), our comparisons revealed topography-generated gravity signals captured [albeit in attenuated form] by the third-generation GOCE gravity field models. This demonstration of GOCE's ability for short-scale signal recovery down to ~80-90 km scales suggests that shortwavelength gravity signals originating from e.g., the crust-mantle boundary and buried anomalous mass loads are captured as well, making the new GOCE data sets a promising source to improve our knowledge on the Earth's lithosphere structure.

823

824 Acknowledgements

We would like to thank the Australian Research Council (ARC) for funding through discovery project grants DP0663020 and DP120102441. CH is the recipient of an ARC Discovery Outstanding Researcher Award (DORA). MK is the recipient of a Curtin Research Fellowship. We also thank the editor and reviewers for their comments on the manuscript, directing us to include isostatic compensation models in this study. We thank ESA for
making the new GOCE gravity fields freely available. Thanks go also to the EGM2008
development team for the topography data. Some figures were produced using the Generic
Mapping Tools (GMT; *Wessel and Smith* [1998]).

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